

PROF. P.C.THOMAS CLASSES & CHAITHANYA CLASSES
KEAM 2020-SOLUTIONS
CODE B1-MATHEMATICS

1. C)

$$f(x) = \sqrt{x-1} \Rightarrow x-1 \geq 0$$

$$x \geq 1$$

$$\Rightarrow [1, \infty)$$

2. D)

$$f(x) = -2x^2 + 1, g(x) = 4x - 3$$

$$(g \circ f)(-1) = g(f(-1))$$

$$= g(-1)$$

$$= -7$$

3. A)

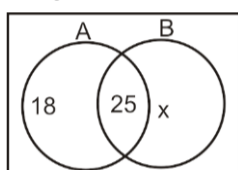
$$18 + 25 + x = 70$$

$$x = 70 - 43$$

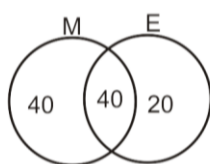
$$x = 27$$

$$n(B) = 27 + 25$$

$$= 52$$



4. C)



$$n(M \cap E) = 40$$

$$n[E \text{ only}] = 20$$

5. B)

$$2 * 5 \frac{2}{5} + \frac{5}{2} + \frac{1}{10} = \frac{4+25+1}{10} = 3$$

6. C)

$$A - B = \{1, 3, 5\}$$

7. B)

$$A = \{2, 3, 4, 5\}$$

$$B = \{36, 45, 49, 60, 77, 90\}$$

$$aRb \Rightarrow a \text{ is a factor of } b$$

8. C)

$$z = e^{3x} \cdot e^{4xi} = e^{3x} [\cos 4x + i \sin 4x]$$

$$\operatorname{Re}(z) = e^{3x} \cos 4x$$

9. A)

$$z = x - iy$$

$$z^{1/3} = p + iq$$

$$z = p^3 + (iq)^3 + 3p^2iq + 3pi^2q^2$$

$$x - iy = p^3 - 3pq^2 + i(3p^2q - q^3)$$

$$x = p[p^2 - 3q^2]$$

$$x = p[p^2 - 3q^2]$$

$$y = q[q^2 - 3p^2]$$

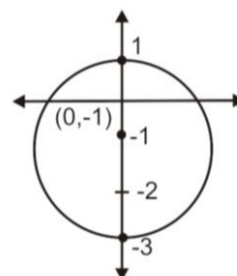
$$\frac{x}{p} + \frac{y}{q} = p^2 + q^2 - 3p^2 - 3q^2$$

$$\frac{x}{p} + \frac{y}{q} = -2(p^2 + q^2)$$

$$\frac{1}{p^2 + q^2} \left(\frac{x}{p} + \frac{y}{q} \right) = -2$$

10. A)

$$|z - -i| = 2 \Rightarrow \text{radius} = 2, \text{centre} = (0, -1)$$



11. D)

$$\alpha = 2 + i$$

$$\beta = 2 - i$$

$$\alpha\beta = 5 = c$$

12. C)

$$\left| \frac{1}{z_1} + \frac{1}{z_2} \right| = \left| \frac{z_1 + z_2}{z_1 z_2} \right| = \frac{|z_1 + z_2|}{|z_1 z_2|} = \frac{3}{4}$$

13. D)

$$z = \frac{1+i}{1-i} = i \Rightarrow \arg(z) = \frac{\pi}{2}$$

14. C)

$$z_1 = 2 + 3i$$

$$z_2 = 3 + 2i$$

$$z_1 + z_2 = 5 + 5i$$

$$|z_1 + z_2| = \sqrt{25 + 25} = \sqrt{50} = 5\sqrt{2}$$

15. D)

$$\frac{10i}{1+2i} = \frac{10i(1-2i)}{5} = 2i(1-2i) = 4 + 2i$$

16. E)

$$\sum_1^{10} (3k^2 + 2k - 1) = 3 \sum_1^{10} k^2 + 2 \sum_1^{10} k - \sum_1^{10} 1$$

$$= \frac{3 \times 10 \times 11 \times 21}{6} + \frac{2 \times 10 \times 11}{2} - 10$$

$$= 1155 + 110 - 10$$

$$= 1255$$

17. C)

$$a_z^2 = a_1 a_6 = a_1 (a_n + 5d)$$

$$(a_1 + d)^2 = a_1^2 + 5a_1 d$$

$$2a_1 d + d^2 = 5a_1 d$$

$$3a_1 d - d^2 = 0$$

$$d[3a_1 - d] = 0$$

$$a \neq 0 \Rightarrow d = 3a_1$$

18. E)

$$a + a + 2d = 6$$

$$2a + 2d = 6$$

$$a + d = 3 \dots (1)$$

$$a + d + a + 3d = 20$$

$$2a + 4d = 20$$

$$a + 2d = 10 \dots (2)$$

$$d = 7, a = -4$$

$$T_{11} = -4 + 70 = 66$$

19. A)

$$\frac{n}{2} [t_1 + t_n] = 70$$

$$n[3 + 17] = 140$$

$$n \times 20 = 140$$

$$n = 7$$

20. D)

$$\frac{1}{30} + \frac{7}{30} + \frac{11}{30} + \frac{13}{30} + \frac{17}{30} + \frac{19}{30} + \frac{23}{30} + \frac{29}{30} = 4$$

21. D)

$$2q = p + 23$$

$$p = 11 \Rightarrow 2q = 11 + 23$$

$$q = 17$$

$$p + q = 11 + 17 = 28$$

22. C)

$$ar^4 = 12$$

$$ar^6 = 48$$

$$r^2 = 4 \Rightarrow r = 2$$

$$ar^8 = 9r^6 \times r^2$$

$$= 48 \times 4$$

$$= 192$$

23. A)

$$1 \rightarrow 10 \Rightarrow S$$

Digits are 1, 3, 5, 7, 9

$$11 \rightarrow 99 \Rightarrow 5 \times 5 = 25$$

$$100 \rightarrow 999 \Rightarrow 5 \times 5 \times 5 = 125$$

24. D)

Polygons can be triangle or quadrilateral or pentagon

$$\text{no} = {}^5C_3 + {}^5C_4 + {}^5C_5$$

$$= 10 + 5 + 1$$

$$= 16$$

25. E)

No. of terms = 21

$$\text{Middle term} = T_{10+1} = {}^{20}C_{10} \left(\frac{1}{5}\right)^{10}$$

26. C)

$${}^{11}C_0 + {}^{11}C_1 + \dots + {}^{11}C_5 =$$

$$\frac{1}{2} [2({}^{11}C_0 + {}^{11}C_1 + {}^{11}C_2 + {}^{11}C_3 + {}^{11}C_4 + {}^{11}C_5)]$$

$$= \frac{1}{2} [{}^{11}C_0 + {}^{11}C_1 + \dots + {}^{11}C_{10} + {}^{11}C_{11}]$$

$$= \frac{1}{2} \times 2^{11} = 2^{10} \quad \boxed{{}^n C_r = {}^n C_{n-r}}$$

27. B)

$$\frac{{}^n P_r}{{}^n C_r} = \frac{840}{35}$$

$$r! = 24$$

$$r = 4$$

28. A)

Put $x = 1$

$$(1 + 2 - 1)^{20} = 2^{20}$$

29. C)

$${}^{10}C_4 = \frac{10 \times 9 \times 8 \times 7}{1 \times 2 \times 3 \times 4} = 210$$

30. D)

$$B = \begin{bmatrix} 62 & 2 \\ 7 & -5 \end{bmatrix} - \begin{bmatrix} -2 & 1 \\ 4 & -9 \end{bmatrix}$$

$$= \begin{bmatrix} 8 & 1 \\ 3 & 4 \end{bmatrix}$$

31. E)

$$\begin{vmatrix} bc & ca & ab \\ a^3 & b^3 & c^3 \\ \frac{1}{a} & \frac{1}{b} & \frac{1}{c} \end{vmatrix} = \frac{1}{abc} \begin{vmatrix} abc & abc & abc \\ a^4 & b^4 & c^4 \\ 1 & 1 & 1 \end{vmatrix} = 0$$

32. C)

$$(24 - 2k) - 2(-18 + 4k) - 1(-6 + 16) = 0$$

$$24 - 2k + 36 - 8k - 10 = 0$$

$$-10k$$

$$50 = 0$$

$$k = 5$$

33. B)

Second Row \times 1st column

34. D)

$$A = \begin{bmatrix} 3 & 4 \\ 5 & 3 \end{bmatrix} \Rightarrow A^{-1} = \frac{1}{9 - 20} \begin{bmatrix} 3 & -4 \\ -5 & 3 \end{bmatrix}$$

$$= \frac{1}{-11} \begin{bmatrix} 3 & -4 \\ -5 & 3 \end{bmatrix}$$

$$= \frac{1}{11} \begin{bmatrix} -3 & 4 \\ 5 & -3 \end{bmatrix}$$

35. A)

$$x + y + 2z = 14 \quad \dots(1)$$

$$3x + 3y + 6z = 17 \dots(2)$$

$$(1) \times 3 \Rightarrow 2x + 3y + 6z = 12 \dots(3)$$

$$(2) - (3) \Rightarrow \quad \quad \quad 0 = 5$$

Not possible

36. C)

$n = 2, 3$, fails

$$n = 5 \Rightarrow \frac{2 \times 5 - 3}{3} \geq \frac{4}{6} + 1 \quad \frac{1}{3} > \frac{1}{6} + 1$$

$$\frac{7}{3} \geq \frac{2}{3} + 1 \quad \frac{7}{3} \geq \frac{4}{6} + 1$$

$$1 + \frac{4}{3} > \frac{2}{3} + 1 \quad 1 + \frac{4}{3} > \frac{2}{3} + 1$$

Which is true

37. A)

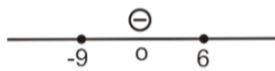
$$|n^2 - 100| < 50$$

$$-50 < n^2 - 100 < 50$$

$$50 < n^2 < 150$$

$$n = 8, 9, 10, 11, 12$$

38. D)



$$[-9, 6)$$

39. B)

40. B)

$$\sin^2 \theta + \cos^2 \theta + \cos^2 \theta = \frac{7}{4}$$

$$\cos^2 \theta = \frac{7}{4} - 1 = \frac{3}{4}$$

$$\cos \theta = \frac{\sqrt{3}}{2} \Rightarrow \theta = 30^\circ$$

41. C)

$$(\sin^2 1 + \sin^2 89) + (\sin^2 2 + \sin^2 88) +$$

$$\dots + (\sin^2 44 + \sin^2 46) + \sin^2 45$$

$$1 + 1 + \dots + 1 + \frac{1}{2}$$

$$= 44 + \frac{1}{2}$$

$$= \frac{89}{2}$$

42. B)

$$\frac{\pi}{2} - \frac{\pi}{8} = \frac{3\pi}{8} \Rightarrow \sin \frac{3\pi}{8} = \cos \frac{\pi}{8}$$

$$\sin \frac{4\pi}{8} + \cos^4 \frac{\pi}{8} = \left(\sin^2 \frac{\pi}{8} + \cos^2 \frac{\pi}{8} \right)^2 - 2 \sin \frac{\pi}{8} \cos^2 \frac{\pi}{8}$$

$$= 1 - \frac{1}{2} \left(2 \sin \frac{\pi}{8} \cos \frac{\pi}{8} \right)$$

$$= 1 - \frac{1}{2} \cdot \sin^2 \frac{\pi}{4} = 1 - \frac{1}{2} \times \frac{1}{2} = 1 - \frac{1}{4} = \frac{3}{4}$$

43. E)

$$\sin(45^\circ + \theta) = \frac{1}{\sqrt{2}} \cos \theta + \frac{1}{\sqrt{2}} \sin \theta$$

$$\cos(45^\circ - \theta) = \frac{1}{\sqrt{2}} \cos \theta + \frac{1}{\sqrt{2}} \sin \theta$$

$$\sin(45^\circ + \theta) - \cos(45^\circ - \theta) = 0$$

44. A)

$$2 \cos^2 x - 1 = \cos x$$

$$2 \cos^2 x - \cos x - 1 = 0$$

$$(2 \cos x + 1)(\cos x - 1) = 0$$

$$\cos x = \frac{-1}{2}, \cos x = 1$$

$$0, \frac{2\pi}{3}$$

$$-2 + 1$$

$$2x^2 - 2x + x - 1$$

$$2x(x-1) + (x-1)$$

$$(x-1)(2x+1)$$

45. B)

$$10 \tan \left[\tan^{-1} \frac{1}{3} + \tan^{-1} \frac{1}{7} \right]$$

$$= 10 \tan \left[\tan^{-1} \left(\frac{\frac{1}{3} + \frac{1}{7}}{1 - \frac{1}{3} \times \frac{1}{7}} \right) \right]$$

$$= 10 \tan \tan^{-1} \left(\frac{10}{20} \right)$$

$$= 10 \times \frac{1}{2} = 5$$

46. E)

$$\tan x + \tan y = \frac{5}{6}, \cot x + \cot y = 5$$

$$\frac{1}{\tan x} + \frac{1}{\tan y} = 5$$

$$\frac{\tan x + \tan y}{\tan x \tan y} = 5$$

$$\frac{5}{6 \times 5} = \tan x \tan y$$

$$\tan x \tan y = \frac{1}{6}$$

$$\tan(x+y) = \frac{\tan x + \tan y}{1 - \tan x \tan y}$$

$$= \frac{\frac{5}{6}}{1 - \frac{1}{6}} = 1$$

47. A)

$$\frac{\sin 91 + \sin 1}{\sin 91 - \sin 1} = \frac{\cos 1 + \sin 1}{\cos 1 - \sin 1}$$

$$= \frac{1 + \tan 1}{1 - \tan 1}$$

$$= \tan(45 + 1)$$

$$= \tan 46$$

48. D)

$$\begin{aligned} & \cos \left[\frac{\pi}{2} + \sin^{-1} \frac{1}{5} \right] \\ & - \sin \sin^{-1} \frac{1}{5} \\ & = -\frac{1}{5} \end{aligned}$$

49. B) $y=7$

50. Out (1,5) in 2 equations

$$5 = m + 2 \Rightarrow m = 3$$

$$\text{also } 5 = a + 5 - 2 \Rightarrow a = 2$$

$$a + m = 5$$

51. E)

$$\frac{2a-5}{9-7} = \frac{25}{5} = 5$$

$$2a - 5 = 5a - 35$$

$$30 = 3a \Rightarrow a = 10$$

52. C)

$$\frac{4}{6} = \frac{6}{k}$$

$$k = 9$$

53. A)

$$y = x + C$$

$$y = 2x - 4$$

$$2y = 2x + 2C$$

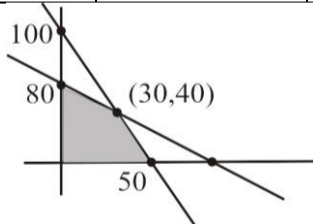
$$y = 2C + 4 \Rightarrow 2 = 2C + 4 \Rightarrow 2C = -2$$

$$C = -1$$

54. D) Vertices

$$z = 7x + 5.4$$

(50,0)	$7 \times 50 + 0$	350
(0,80)	$0 + 400$	400
(30,40)	$210 + 200$	410



55. E)

$$r^2 = 4^2 + 5^2 = 41$$

$$(x-3)^2 + (y-6)^2 = 41$$

$$x^2 + y^2 - 6x - 12y + 4 = 0$$

56. C)

$$x^2 + y^2 - 5x + 2y = 0$$

$$(-y, -f) = (2, -1)$$

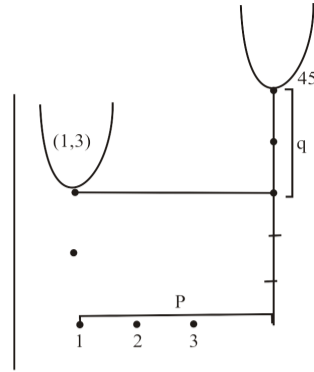
$$r = \sqrt{2^2 + 1^2} = \sqrt{5}$$

57. B) Centre = (4-3) $r = \sqrt{7}$

$$(x-4)^2 + (y+3)^2 = 7$$

$$x^2 + y^2 - 8x + 6y + 18 = 0$$

58. D)



$$y = x^2 - 2x + 1 + 3$$

$$= (x-1)^2 + 3$$

$$p = 3,$$

$$q = 2$$

59. B)

$$y = x^2 - 10x + 16 + 7$$

$$y = x^2 - 10x + 23$$

$$y = x^2 - 10x + 25 - 2$$

$$y = (x-5)^2 - 2$$

$$(5, -2)$$

60. C)

$$400x^2 + 100y^2 = 40000$$

$$4x^2 + y^2 = 400$$

$$\frac{x^2}{100} + \frac{y^2}{400} = 1$$

$$\frac{x^2}{10^2} + \frac{y^2}{20^2} = 1$$

$$a = 20, b = 10$$

$$2a = 40, 2b = 20$$

61. D)

$$\frac{x^2}{1^2} + \frac{y^2}{2^2} = 1$$

$$a^2 = 4, b^2 = 1$$

$$e = \sqrt{1 - \frac{b^2}{a^2}} = \sqrt{1 - \frac{1}{4}} = \frac{\sqrt{3}}{2}$$

62. E) $\frac{x^2}{2} - \frac{y^2}{3} = 1$

$$\frac{2b^2}{a} = \frac{2 \times 3}{\sqrt{2}} = 3\sqrt{2}$$

63. B)

$$|\vec{u} \times \vec{v}|^2 = |\vec{u}|^2 |\vec{v}|^2 \sin^2 \theta$$

$$|\vec{u} \cdot \vec{v}|^2 = |\vec{u}|^2 |\vec{v}|^2 \cos^2 \theta$$

$$|\vec{u} \times \vec{v}|^2 + |\vec{u} \cdot \vec{v}|^2 = |\vec{u}|^2 |\vec{v}|^2$$

$$14 \times 45$$

$$= 630$$

64. B)

$$|\vec{a}| = \sqrt{1 + 25 + 64} = \sqrt{90} = 3\sqrt{10}$$

$$d\vec{e} = \left\langle \frac{1}{3510}, \frac{-5}{3\sqrt{10}}, \frac{8}{3\sqrt{10}} \right\rangle$$

65. B)

$$\cos \theta = \frac{2+3-1}{\sqrt{3}\sqrt{14}} = \frac{4}{\sqrt{42}}$$

$$\tan \theta = \frac{\sqrt{26}}{4}$$

66. D)

$$\perp r \Rightarrow \vec{a} \cdot \vec{b} = 0$$

$$6 - 2\lambda = 0 \Rightarrow \lambda = 3$$

67. E)

$$\sqrt{a^2 + (\alpha + 1)^2 + 4} = 3$$

$$2a^2 + 2a + 5 = 9$$

$$2a^2 + 2a - 4 = 0$$

$$a^2 + a - 2 = 0$$

$$(\alpha + 2)(\alpha - 1) = 0$$

$$\alpha = -2, 1$$

68. D)

$$(\vec{a} + \vec{b}) \cdot (\vec{a} - \vec{b}) = |\vec{a}|^2 - |\vec{b}|^2$$

$$= 17 - 6$$

$$= 11$$

69. E)

$$\frac{\vec{a} \cdot \vec{b}}{|\vec{b}|} = \frac{\vec{b} \cdot \vec{a}}{|\vec{a}|} \Rightarrow |\vec{a}| = |\vec{b}|$$

$$\Rightarrow 1 + 4 + 9 = \lambda^2 + 9$$

$$\Rightarrow \lambda^2 = 5$$

$$\Rightarrow \lambda = \pm \sqrt{5}$$

70. A)

$$[\vec{a} - \vec{b}]^2 = |\vec{a}|^2 - |\vec{b}|^2 - 2\vec{a} \cdot \vec{b}$$

$$= 4 + 9 - 2 \times 4$$

$$= 5$$

$$[\vec{a} - \vec{b}] = \sqrt{5}$$

71. D) Substituting

$$(3, 3, 0) \Rightarrow \frac{3-1}{2} = 1$$

$$\frac{3+1}{4} = 1$$

$$\frac{0-2}{-2} = 1$$

72. B)

$$\vec{r}, \vec{n} = \vec{a} \cdot \vec{r}$$

$$(\hat{i} + \hat{j} + 8\hat{k}) \cdot (\hat{i} + \hat{j} + \hat{k}) = (\hat{j} + \hat{k}) \cdot (\hat{i} + \hat{j} + \hat{k})$$

$$x + 9 + z = 2$$

73. C)

$$PM = \left| \frac{6 \times 4 + 2 \times 2 - 3 \times 9 - 46}{\sqrt{6^2 + 2^2 - 9^2}} \right|$$

$$= \left| \frac{24 + 4 - 27 - 46}{11} \right|$$

$$= \frac{45}{11}$$

74. C) $3x + y + 2z = 18$

$$\frac{x}{6} + \frac{y}{18} + \frac{z}{9} = 1$$

$$a + b + c = 6 + 18 + 9 = 33$$

75. A) At xy plane, $z = 0$ (Using parametric equation)

$$z = 4\lambda - 3 = 0 \Rightarrow \lambda = \frac{3}{4}$$

$$x = \lambda + 2 = \frac{3}{4} + 2 = \frac{11}{4}$$

$$y = -5\lambda + 4 = \frac{-15}{4} + 4 = \frac{1}{4}$$

76. D)

$$dr = \langle 6, 1, 3 \rangle, \text{ only D satisfy}$$

77. A)

$$\cos \theta = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}| \cdot |\vec{b}|} = \frac{1 - 2 + 3}{\sqrt{3} \sqrt{14}}$$

$$= \frac{2}{\sqrt{42}}$$

78. E)

$$\pi_1 + \lambda \pi_2 = 0$$

$$(x + 2y - z - 3) + \lambda(x + 4 - 3z - 5) = 0,$$

$$p^* (1 - 1, 0)$$

$$(1 - 2 - 3) + \lambda(1 - 1 - 5) = 0$$

$$-4 - 5\lambda = 0 \quad \lambda = \frac{4}{5}$$

$$(x + 2y - z - 3) - \frac{4}{5}(x + 4 - 3z - 5) = 0$$

$$x + 6y + 7z + 5 = 0$$

79. D)

$$\frac{\sum x}{30} = 80 \Rightarrow \sum x = 2400$$

$$\frac{\sum x - (x_1 + x_2)}{28} = 82$$

$$2400 - (x_1 + x_2) = 82 \times 28$$

$$x_1 + x_2 = 2400 - 2296$$

$$x_1 + x_2 = 104$$

$$\frac{x_1 + x_2}{2} = 52$$

80. A)

$$S = \{2, 3, 5, 7, 11, 13\}$$

Sum is a prime no.

Favourable eases are

$$(2, 3), (3, 2), (2, 5), (9, 2), (2, 11), (11, 2)$$

$$\therefore P = \frac{6}{36} = \frac{1}{6}$$

81. E)

$$A = \{1, 2, 3, 4, 5\}$$

$$n(s) = S_{C_5} = 10$$

$$AP: d = 1 \Rightarrow 3 \text{ cases } (1, 2, 3), (2, 3, 4), (3, 4, 5)$$

$$d = 2 \Rightarrow 1 \text{ case, } (1, 3, 5)$$

$$P = \frac{4}{10} = \frac{2}{5}$$

82. C) Let total no - 100

$$n_1 = 20, \bar{x}_1 = 70, n_2 = 40, \bar{x}_2 = 80$$

$$n_3 = 30, \bar{x}_3 = 90, n_4 = 10, \bar{x}_4 = 100$$

$$\bar{x} = \frac{n_1\bar{x}_1 + n_2\bar{x}_2 + n_3\bar{x}_3 + n_4\bar{x}_4}{n_1 + n_2 + n_3 + n_4}$$

$$= \frac{1400 + 3200 + 2700 + 1000}{100}$$

$$= 83$$

83. B)

$$P(A \cup B) = P(A) + P(B)$$

$$P(B) = (A \cup B) - P(A)$$

$$= 0.75 - 0.5$$

$$= 0.25$$

84. B)

$$P(R) = \frac{n(R)}{n(S)} = \frac{3}{20}$$

85. E)

$$\sum P(X) = 1 \Rightarrow 15a = 1 \Rightarrow a = \frac{1}{15}$$

$$E(X) = \sum x_i p_i = -a + 0 + 3a + 8a + 15a$$

$$= 25a$$

$$= \frac{25}{15} = \frac{5}{3}$$

86. B)

$$-2 \leq x \leq 1 \Rightarrow f(x) = x^2 - 2x$$

$$f(-1) = 1 + 2 = 3$$

87. A)

$$\frac{dy}{dx} = \frac{2x - y}{x + 2y} = \frac{2 - \frac{y}{x}}{1 + 2\frac{y}{x}} \quad y = vx$$

$$V + x \frac{dV}{dx} = \frac{2 - V}{1 + 2V}$$

$$\frac{xdV}{dx} = \frac{2 - V}{1 + 2V} - V = \frac{2 - V - V(1 + 2V)}{1 + 2V}$$

$$x \frac{dV}{dx} = \frac{2 - V - V - 2V^2}{1 + 2V} = \frac{2(1 - v - v^2)}{1 + 2v}$$

$$x \frac{dV}{dx} = \frac{-2[V^2 + V - 1]}{2V + 1}$$

$$\frac{(2V + 1)dV}{V^2 + V - 1} = \frac{-2dx}{x}$$

$$\log(V^2 + V - 1) = -2 \log x + \log C$$

$$\log\left(\frac{y^2}{x^2} + \frac{y}{x} - 1\right) = \log \frac{C}{x^2} +$$

$$\frac{y^2 + xy - x^2}{x^2} = \frac{C}{x^2}$$

$$x^2 - y^2 - xy = C$$

88. E)

$$\lim_{x \rightarrow 3} \frac{e^{x-3} - x + 1}{x^2 - \log(x-2)} = \frac{e^0 - 3 + 1}{9 - \log 1} = \frac{2-3}{9} = \frac{-1}{9}$$

89. E) $\lim_{x \rightarrow 4} \frac{\sqrt{x^2 + 9} - 5}{x - 4} = \lim_{x \rightarrow 4} \frac{1 \times 2x}{2\sqrt{x^2 + 9}}$

$$= \frac{4}{5}$$

90. D) LHL = RHL

$$\Rightarrow 4C + 4 = 8$$

$$\Rightarrow 4C = 4$$

$$\Rightarrow C = 1$$

91. A)

$$\lim_{x \rightarrow 0} \frac{x^{100} \cdot \sin 7x}{(\sin x)^{100} \cdot \sin x}$$

$$\frac{\sin 7x}{7x} \times 7x$$

$$\lim_{x \rightarrow 0} \frac{7x}{\frac{\sin x}{x}} = 7$$

92. B)

$$f(x) = \frac{5}{2}x^2 - e^x$$

$$f'(x) = 2 \times \frac{5}{2}x = e^x$$

$$f''(x) = 5 - e^x$$

$$f''(x) = 0 \Rightarrow e^x = 5 \Rightarrow x = \log 5$$

93. E)

$$y = (\cos x)^{2x}$$

$$\log y = 2x \log(\cos x)$$

$$\frac{1}{y} \cdot \frac{dy}{dx} = \frac{2x(-\sin x)}{\cos x} + \log \cos x \cdot 2$$

$$\frac{dy}{dx} = 2(\cos x)^{2x} [\log \cos x - x \tan x]$$

94. A)

$$x^3 + 2xy + \frac{y^3}{3} = \frac{11}{3}$$

$$3x^2 + 2xy' + y \times 2 + \frac{3y^2}{3}y' = 0, x = 2, y_2 = -1$$

$$12 + 4y' - 2 + y' = 0$$

$$5y' + 10 = 0$$

$$y' = -2$$

95. C)

$$x > 3 \Rightarrow f(x) = 5 - 2x$$

$$f'(x) = -2 \Rightarrow f'(6) = -2$$

96. E) $F(x) = (f(g(x)))^2$

$$F'(x) = 2f(g(x)) \cdot f'(g(x)) \cdot g'(x)$$

$$F'(1) = 2f(2) \cdot f'(2) \cdot 3$$

$$= 2 \times 4 \times 5 \times 3 = 120$$

97. C) $y = 2 + \sqrt{u}$

$$\frac{dy}{dx} = \frac{1}{2\sqrt{u}} \times \frac{du}{dx}, \quad \frac{dy}{dx} = 3x^2$$

$$= \frac{3x^2}{2\sqrt{x^3 + 1}}$$

98. B)

$$y = -2x^2 + 3$$

$$\frac{dy}{dx} = -4x \Rightarrow m = -4$$

$$x = 1 \Rightarrow y = 1 \Rightarrow (x_1, y_1) = (1, 1)$$

Eqn. of tangent

$$(y - 1) = -4(x - 1)$$

$$y - 1 = -4x + 4$$

$$y = -4x + 5$$

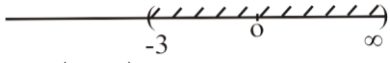
99. C)

$$f(x) = x^3 e^x$$

$$f'(x) = e^x [x^3 + 3x^2]$$

$$f'(x) = 0 \Rightarrow x^2(x+3) = 0$$

$$\Rightarrow x = 0, x = -3$$



$$(-3, \infty)$$

100.B)

L.M.V.T

$$f'(c) = \frac{f(b) - f(a)}{b - a}$$

$$\frac{1}{2\sqrt{c}} = \frac{4-2}{16-4} = \frac{2}{12} = \frac{1}{6}$$

$$2\sqrt{c} = 6$$

$$\sqrt{c} = 3$$

$$c = 9$$

101.E)

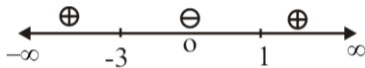
$$f(x) = (x^2 - 3)e^x$$

$$f'(x) = e^x [x^2 - 3 + 2x]$$

$$f'(x) = 0 \Rightarrow x^2 + 2x - 3 = 0$$

$$\Rightarrow (x+3)(x-1) = 0$$

$$\Rightarrow x = -3, 1$$



$$f'(x) < 0 \Rightarrow x \in (-3, 1)$$

102.A)

$$y = \frac{2}{x^2} \quad x = 1 \Rightarrow y = 2$$

$$\frac{dy}{dx} = \frac{-4}{x^3}, m = -4 \Rightarrow m_2 = \frac{1}{4}$$

$$y - 2 = \frac{1}{4}(x - 1)$$

$$4y - 8 = x - 1$$

$$x - 4y + 7 = 0$$

103.C)

$$f(x) = x^2 - x$$

$$f'(x) = 2x - 1$$

$$f'(x) = 0 \Rightarrow x = \frac{1}{2}$$

$$f\left(\frac{1}{2}\right) = \frac{1}{4} - \frac{1}{2} = -\frac{1}{4}$$

104.A)

$$\int 3x^2 (x^3 + 1)^{10} dx = \int t^{10} dt, \quad t = (x^3 + 1)$$

$$-\frac{t^{11}}{11} + C$$

$$= \frac{(x^3 + 1)^{11}}{11} + C$$

105.E)

$$\int \frac{2x + \sin 2x}{1 + \cos 2x} dx = \int \frac{2x + 2 \sin x \cos x}{2 \cos^2 x} dx$$

$$= \int (x \sec^2 x + \tan x) dx$$

$$= \int d(x \tan x)$$

$$= x \tan x + C$$

$$106.D) \quad \int \frac{1}{x^2 - 5^2} dx = \frac{1}{2 \times 5} \log \left| \frac{x-5}{x+5} \right| + C$$

$$107.A) \quad \int \frac{\left(\frac{1}{x}\right)}{\log x} dx = \log |\log x| + C$$

108.E)

$$\int e^x [\sec x + \sec x \tan x] dx$$

$$= e^x \sec x + c$$

109.D)

$$\int \frac{dx}{\sqrt{x}(1+\sqrt{x})} \quad t = 1 + \sqrt{x}$$

$$dt = \frac{1}{2\sqrt{x}} dx$$

$$= \int \frac{2dt}{t}$$

$$= 2 \log |t| + c$$

$$= 2 \log |1 + \sqrt{x}| + c$$

110.A)

$$\int \sec^2(5x-1) dx = \frac{\tan(5x-1)}{5}$$

111.B)

$$I = \int_0^{\pi/2} \frac{1}{1 + \frac{\cos^4 x}{\sin^4 x}} dx$$

$$= \int_0^{\pi/2} \frac{\sin^4 x}{\sin^4 x + \cos^4 x} dx = \frac{\pi}{4}$$

112.B)

$$\int_{-a}^a f(x) dx = 0 \quad \text{if } f(x) \text{ is odd}$$

x^3 and x are odd function

$$\therefore \int_{-10}^{10} 20 dx = 20 [x]_{-10}^{10} = 20 \times 20 = 400$$

113.D)

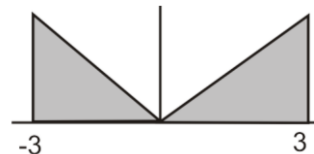
$$\frac{x}{3} = \cos \theta$$

$$\frac{y}{2} = \sin \theta$$

$\frac{x^2}{9} + \frac{y^2}{4} = 1 \Rightarrow$ (curve is ellipse in first and 2nd quadrant)

$$\text{area} = \frac{\pi ab}{2} = \frac{\pi \times 3 \times 2}{2} = 3\pi$$

114.D)



$$y = |x|$$

$$\text{Area} = 2 \times \frac{1}{2} \times 3 \times 3 = 9$$

115. B)

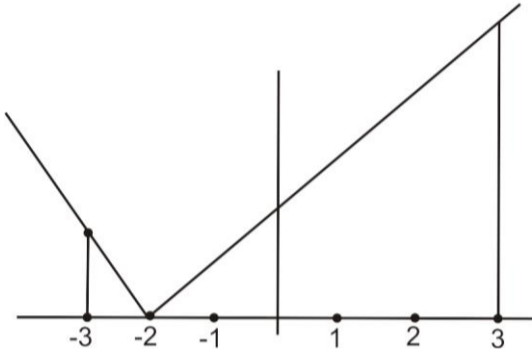
$$\int_e^{e^2} \frac{1}{x} dx = [\log(x)]_e^{e^2}$$

$$= \log e^2 - \log e$$

$$= 2 - 1$$

$$= 1$$

116.D)



$$\int_{-3}^3 |x+2| dx$$

$$\text{area} = \frac{1}{2} + \frac{25}{2} = 13$$

117.A)

Order 2, degree = 4

$$\frac{d^2y}{dx^2} = -\sqrt{x^2 + \left(\frac{dy}{dx}\right)^{3/2}}$$

$$\left(\frac{d^2y}{dx^2}\right)^2 = x^2 + \left(\frac{dy}{dx}\right)^{3/2}$$

$$\left[\left(\frac{d^2y}{dx^2}\right)^2 - x^2\right]^2 = \left(\frac{dy}{dx}\right)^3$$

118.E)

$$\frac{dy}{dx} + \frac{y}{x} = x$$

$$\text{I.F} = e^{\int \frac{1}{x} dx} = e^{\log x} = x$$

$$yx = \int x \cdot x dx$$

$$yx = \frac{x^3}{3} + C$$

$$y = \frac{x^2}{3} + \frac{C}{x}$$

119.C)

$$y' - \frac{1}{3x}y = \frac{1 + \log x}{3x}$$

$$\text{I.F} = e^{\int -\frac{1}{3x} dx} = e^{-\frac{1}{3} \log x}$$

$$= e^{\log x^{-\frac{1}{3}}}$$

$$= x^{-1/3}$$

120.A)

$$y = \frac{A}{x} + B$$

$$y' = \frac{-A}{x^2}$$

$$y'x^2 = -A$$

$$x^2y'' + y'2x = 0 \text{ Dividing by } x$$

$$x \frac{d^2y}{dx^2} + 2 \frac{dy}{dx} = 0$$
